

# Mechanistic Insight into the Chemiluminescent Decomposition of Firefly Dioxetanone

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Supporting Information

**ABSTRACT:** The peroxide decomposition that generates the excited-state carbonyl compound is the key step in most organic chemiluminescence, and chemically initiated electron exchange luminescence (CIEEL) has been widely accepted for decades as the general mechanism for this decomposition. The firefly dioxetanone, which is a peroxide, is the intermediate in firefly bioluminescence, and its decomposition is the most



important step leading to the emission of visible light by a firefly. However, the firefly dioxetanone decomposition mechanism has never been explored at a reliable theoretical level, because the decomposition process includes biradical, charge-transfer (CT) and several nearly degenerate states. Herein, we have investigated the thermolysis of firefly dioxetanone in its neutral (FDOH) and anionic (FDO<sup>-</sup>) forms using second-order multiconfigurational perturbation theories in combination with the ground-state intrinsic reaction coordinate calculated via the combined hybrid functional with Coulomb attenuated exchange-correlation, and considered the solvent effect on the ground-state reaction path using the combined hybrid functional with Coulomb attenuated exchange-correlation. The calculated results indicate that the chemiluminescent decomposition of FDOH or FDO<sup>-</sup> does not take place via the CIEEL mechanism. An entropic trap was found to lead to an excited-state carbonyl compound for FDOH, and a gradually reversible CT initiated luminescence (GRCTIL) was proposed as a new mechanism for the decomposition of FDO<sup>-</sup>.

# ■ INTRODUCTION

A firefly's emission of visible light is the most well-known bioluminescence in nature due to its highly efficient luminescence (the quantum yield is  $0.41^{1}$ ). The accepted process for the firefly bioluminescence involves reactions of Dluciferin, ATP, and O2 to produce oxyluciferin. The light emission is thought to occur via the formation of D-luciferyl adenylate and the high-energy dioxetanone intermediate (Int). The thermolysis of the high-energy Int, firefly dioxetanone (FDO), was suggested to produce  $CO_2$  in the ground state  $(S_0)$ and part of oxyluciferin in the first excited singlet state  $(S_1)$  (see Scheme 1). Subsequently, the  $S_1$  state of oxyluciferin decays to its S<sub>0</sub> state and emits visible light. The S<sub>1</sub> to S<sub>0</sub> transition has been extensively studied experimentally<sup>2</sup> and theoretically<sup>3,4</sup> in the gas phase, solvent, and protein. As pointed out by Koo and Schuster in 1977, "In general, the exothermic decomposition of peroxides to generate directly electronically excited-state carbonyl compounds has formed the basis for nearly all of organic chemiluminescence."<sup>5</sup> It is obvious that the thermolysis of FDO is the key step for firefly bioluminescence. However, the thermolysis of FDO has not been studied at a reliable theoretical level even though the decomposition of simple 1,2dioxetane and dioxetanones has been extensively studied experimentally<sup>6,7</sup> and theoretically.<sup>8</sup> Moreover, the decomposition of firefly dioxetanone in the firefly bioluminescence cannot be directly observed. Therefore, the theoretical investigation of the decomposition process will play a unique role in understanding firefly bioluminescence. FDO might exist in its neutral (FDOH) and anionic (FDO<sup>-</sup>) forms (see Chart 1) in the protein environment. The decomposition of both forms has to be studied simultaneously to explore the chemiluminescence mechanism and efficiency.

Small analogues of **FDOH** have been extensively studied theoretically.<sup>4a,8f,g,9</sup> Multiconfigurational calculations have shown that the decomposition of 1,2-dioxetane,<sup>8e</sup> 1,2-dioxetanoe,<sup>8f</sup> and the thiazole-substituted dioxetanone<sup>8g</sup> occurs via a typical stepwise mechanism involving one excited-state Int and two discrete transition states (TSs) along the reaction path. However, only one TS was located on the decomposition pathway of thiazole-substituted dioxetano-ne<sup>4a</sup> and FDOH<sup>10</sup> using B3LYP calculations. It is well-known that the B3LYP calculation of charge-transfer (CT) states<sup>11</sup> and could "lead to a complete misunderstanding of the underlying physical mechanisms,"<sup>12</sup> because this method employs the incorrect long-range form of the exchange correlation functional.

The results from several semiempirical<sup>4a,13</sup> and DFT<sup>10,14</sup> studies of the decomposition of **FDO**<sup>-</sup> (see Chart 1) have been reported for the decomposition process of the S<sub>0</sub> state. The only multiconfigurational calculation for this decomposition process was performed by Chung et al.<sup>15</sup> in 2008. They performed a complete active space self-consistent (CASSCF)<sup>16</sup>

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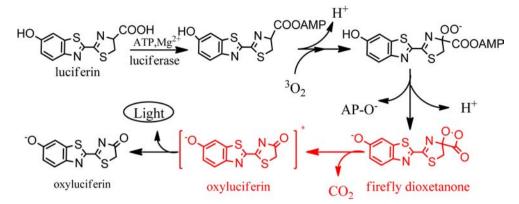
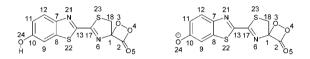


Chart 1. Firefly Dioxetanone in Neutral (FDOH) and Anionic (FDO $^-$ ) Forms



calculation consisting of an active space of 12 active electrons in 12 active orbitals (12-in-12). One TS and a seam of sloped conical intersections (CI) were determined and used to explain the highly efficient luminescence. In their calculation, the 4-in-4 active space is used for the dioxetanone moiety, but the exclusion of the carbonyl oxygen's p orbitals is likely to be insufficient.8f,g In fact, the p orbitals contribute more to the electron transfer (ET) during the cleavage of the O-O bond in our current calculations. Greenman and Mazziotti suggested an accurate calculation of the strong electron correlation in FDO<sup>-</sup> will likely require an active space of 28-in-25.<sup>17</sup> In the whole  $\pi$ system of FDO-, except those orbitals related to ET mechanism, the others do not change significantly during the decomposition of FDO<sup>-</sup> and do not have to be included in the active space, resulting in a smaller but suffice active space in this Article.

To explain the chemiluminescence of FDO (FDOH and FDO<sup>-</sup>), the intramolecular chemically initiated electronexchange luminescence (CIEEL) mechanism was proposed in the 1970s<sup>5,6e,18</sup> and is widely accepted as the mechanism for firefly bioluminescence. In the CIEEL mechanism, the decomposition is first initiated by ET from the electron donor to the peroxide bond forming a neutral radical/anionic radical pair followed by a subsequent back electron transfer (BET) between the radicals that releases enough energy to promote the fluorophore to its  $S_1$  state. However, there is some doubt regarding the existence of such a BET<sup>8a,10,19</sup> and the efficiency of the BET process between the radicals in a solvent cage.<sup>19a,ć</sup> Another explanation for the decomposition of FDO involves the CT initiated luminescence (CTIL) mecha-nism,<sup>10,19,20</sup> which consists of the rate-determining endothermic formation of a TS with CT characteristics and the subsequent reaction occurs via a CI producing excited-state product. Recently, the intramolecular charge-transfer-induced decomposition (CTID) mechanism was proposed,<sup>21</sup> which is more encompassing and includes the CIEEL and other CTinduced mechanisms. The mechanistic controversy stems from the challenge of characterizing the decomposition of FDO at the molecular level. Herein, the primary goal is to simulate the decomposition process of FDOH and FDO- using quantum

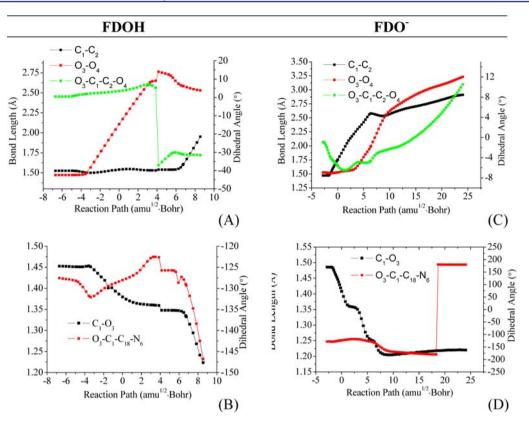
chemical methods at a reliable level and to elucidate the chemiluminescent mechanism.

First, the computational methodology is described followed by the detailed results of the thermolysis of **FDOH** and **FDO**<sup>-</sup> in gas and solution phases. Subsequently, the discussion on the decomposition mechanism of **FDOH** and **FDO**<sup>-</sup> is presented including the proposal of the gradually reversible CT initiated luminescence (GRCTIL) mechanism, solvent effects, and activation energy. Finally, the main conclusions are briefly summarized. The report is supplemented by Supporting Information providing additional information and details.

## COMPUTATIONAL DETAILS

Yanai et al. combined the features of the B3LYP hybrid functional with the long-range corrected functional to create a new Coulomb attenuated hybrid exchange-correlation functional (CAM-B3LYP),<sup>22</sup> which improves the description of CT excitations.<sup>23</sup> We theoretically investigated the thermolysis mechanism of FDOH and FDO<sup>-</sup> using a combined method. The CAM-B3LYP and the second-order multiconfigurational perturbation (CASPT2)<sup>24</sup> methods were employed to investigate the geometric relaxation and energetics during the decomposition process, respectively. For comparison, the energies of several excited states were also calculated using the time-dependent (TD) CAM-B3LYP method. The unrestricted open-shell CAM-B3LYP (UCAM-B3LYP) method was employed to calculate the intrinsic reaction coordinate (IRC), to optimize the stationary points (i.e., minimum (Min), TS, and Int), and to analyze the frequencies of these points to characterize their nature. As Johnson et al. stated, the geometric optimization using B3LYP is reliable even though it exhibits a systematic error for the prediction of the thermochemistry of the studied reactions.<sup>25</sup> Broken-symmetry (BS) technology that mixes the HOMO and LUMO orbitals for the initial guess orbitals was employed for the biradical states. The spin-contamination in the BS wave function was treated using Yamaguchi's formula.<sup>26</sup> The details are provided in the Supporting Information. The Mulliken population analysis was employed to identify the CT characteristics. The 6-31G\*\* basis set<sup>27</sup> was employed for all of the CAM-B3LYP and TD CAM-B3LYP calculations. The larger basis sets, which included 6-31+G\*\* and 6-31++G\*\*, have been tested and showed no improvement in the geometry optimization (see Figure S1, Supporting Information). All of these density functional theory (DFT) calculations were performed with the Gaussian 09 program suite.<sup>24</sup>

The CASPT2<sup>24</sup> method was employed to calculate the energies at the CAM-B3LYP optimized geometries. The ANO-RCC basis sets<sup>29</sup> with a contraction scheme of [3s2p1d] for carbon, nitrogen, and oxygen, [4s3p1d] for sulfur, and [2s1p] for hydrogen, which is designated ANO-RCC-VDZP, were employed in the CASPT2 calculations. The valid active space has been extensively checked. The 16-in-13 for the **FDOH** and 18-in-15 for the **FDO<sup>-</sup>** were chosen (see the Supporting Information for the specific description of the



**Figure 1.** The structural change of  $C_1-C_2$ ,  $O_3-O_4$ ,  $O_3-C_1-C_2-O_4$ ,  $C_1-O_3$ , and  $O_3-C_1-C_{18}-N_6$  of the  $S_0$  state along the reaction path calculated by (TD) (BS)-UCAM-B3LYP method of **FDOH** (left) and **FDO**<sup>-</sup> (right).

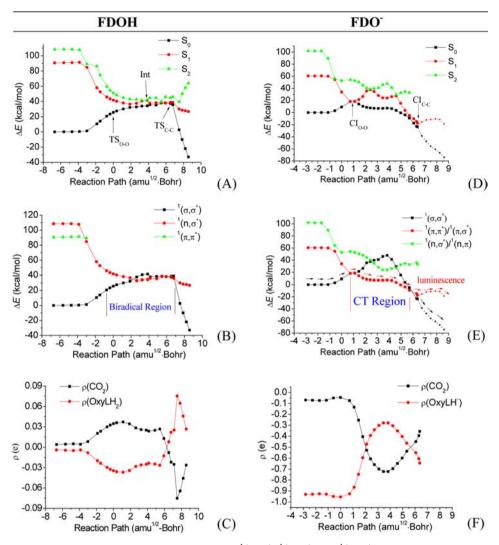
active spaces). To hold the integrity of the active space throughout the whole reaction process, the state-average (SA) technique was employed to consider six roots simultaneously. However, only the lowest three singlet and one triplet states are important. Therefore, the results of the higher states were not considered. All of these calculations except the CI optimization were performed with MOLCAS 7.6.<sup>30</sup> The CI optimizations were performed with Molpro  $2010^{31}$  at the SA-CASSCF/6-31G\*\* level.

For **FDOH** and **FDO**<sup>-</sup>, the DFT solvent optimized geometries do not differ significantly from those in the gas phase.<sup>10</sup> Therefore, we only performed the single-point energy correction for the gas-phase optimized geometries when considering solvent effects. Two solvents with different dielectric constant ( $\varepsilon$ ) were employed including a nonpolar solvent, benzene ( $\varepsilon = 2.25$ , close to the  $\varepsilon$  value of the real biosystem, whose  $\varepsilon$  is 2.5–4), and a polar solvent, DMSO ( $\varepsilon = 46.70$ ), which is generally used in the chemiluminescence reaction.<sup>32</sup> The polarizable continuum model (PCM)<sup>33</sup> was employed for the nonpolar solvent, benzene, and the conductor-like polarized continuum model (C-PCM)<sup>34</sup> was employed for the polar solvent, DMSO, in the self-consistent reaction field calculations.

# RESULTS

The important geometric parameters of the stationary points on the  $S_0$  adiabatic potential energy surfaces (PESs) of **FDOH** and **FDO**<sup>-</sup> are listed in Table S1. The relative energies of these points were calculated using the CASPT2 methods and are listed in Table S2. The corresponding occupation number for important orbitals of Min, Int,  $TS_{O-O}$ , and  $TS_{C-C}$  of **FDOH** as well as Min,  $TS_{O-O}$ ,  $CI_{O-O}$ , and  $CI_{C-C}$  of **FDO**<sup>-</sup> calculated using the CAM-B3LYP or CASSCF method are shown in Figures S2–S10.  $TS_{O-O}$  and  $TS_{C-C}$  are the TSs corresponding to O–O breaking and C–C breaking, respectively. The potential energy curves (PECs) for the **FDOH** and **FDO**<sup>-</sup> ground and excited states calculated using the TD (BS)- UCAM-B3LYP method are shown in Figure S11, together with the charge population of the CO<sub>2</sub> moiety and the other moiety (OxyLH<sub>2</sub> for **FDOH** and OxyLH<sup>-</sup> for **FDO**<sup>-</sup>) along the reaction path. The changes in the key geometric parameters along the reaction path are shown in Figure 1. Table S3 summarized the important geometric parameters of the minima and TSs of **FDOH** and **FDO**<sup>-</sup> optimized by the current CAM-B3LYP and the previous B3LYP methods.<sup>10</sup> The plot of **FDOH** PECs is similar to the previously calculated ones of 1,2dioxetane,<sup>8e</sup> 1,2-dioxetanone,<sup>8f</sup> neutral thiazole-substituted dioxetanone,<sup>8g</sup> and phenol-substituted dioxetanone.<sup>10</sup> The plot of **FDO**<sup>-</sup> PECs is similar to the previously calculated anionic thiazole-substituted dioxetanone.<sup>8g</sup> and phenol-substituted dioxetanone.<sup>10</sup> Detailes of **FDOH** and **FDO**<sup>-</sup> PECs are depicted below.

For FDOH, near the Min structure,  $S_0$  is of a typical Hartree-Fock closed-shell configuration, and the S1 and T1 states are the  $\pi \to \pi^*$  transition from the p- $\pi$  conjugating orbital (the p orbital of  $O_{24}$  and the  $\pi$  orbital of the benzothiazol) to the  $\pi^*$  of  $N_{21}$ - $C_{13}$ - $C_{17}$ - $N_6$  with no obvious CT characteristics. With the stretching of the  $O_3-O_4$  bond, the  $\sigma$  and  $\sigma^*$  orbitals are moving closer in energy, and the transition characteristics of the S<sub>1</sub> and T<sub>1</sub> states are changed from  $(\pi, \pi^*)$ to  $(n_{\sigma}\sigma^{*})$ , which is from the nonbonding orbital of O<sub>3</sub> to the  $\sigma^{*}$ of O<sub>3</sub>-O<sub>4</sub>. We denoted the three lowest single and one triplet states as  ${}^{1}(\sigma,\sigma^{*})$ ,  ${}^{1}(n,\sigma^{*})$ ,  ${}^{1}(\pi,\pi^{*})$ , and  ${}^{3}(n,\sigma^{*})$ , respectively. The adiabatic and diabatic PECs and the population of the Mulliken charges on the CO<sub>2</sub> and OxyLH<sub>2</sub> moieties of FDOH were calculated using the CASPT2//CAM-B3LYP method and are described on the left side of Figure 2. For convenience, the diabatic PECs are used in the discussion below. As shown in



**Figure 2.** The PECs of the S<sub>0</sub>, S<sub>1</sub>, and S<sub>2</sub> adiabatic states, the diabatic  $(\sigma,\sigma^*)$ ,  $(n,\sigma^*)$ , and  $(\pi,\pi^*)$  states, the population of Mulliken charges on CO<sub>2</sub>, and the OxyLH<sub>2</sub>/OxyLH<sup>-</sup> moieties of the S<sub>0</sub> state in the gas phase calculated by the CASPT2//CAM-B3LYP method of **FDOH** (left) and **FDO**<sup>-</sup> (right).

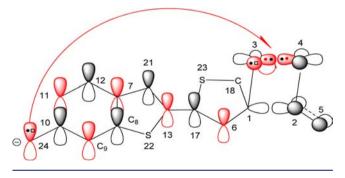
Figure 2B, the  ${}^{1}(\pi,\pi^*)$  state is not involved in the lowest six roots after IRC =  $-3.01 \text{ amu}^{1/2}$  bohr.

For **FDO**<sup>-</sup>, the characteristics of the S<sub>0</sub>, S<sub>1</sub>, and T<sub>1</sub> states at the S<sub>0</sub> Min are the same as observed for **FDOH**. However, with the O<sub>3</sub>-O<sub>4</sub> stretching, the  $\pi^*$  orbital couples with the  $\sigma^*$ orbital, and the S<sub>1</sub> and T<sub>1</sub> states become a  $\pi \to \sigma^*$  transition with a typical CT characteristic (see Chart S1). However, the electronic state may change among (n, $\sigma^*$ ), ( $\sigma$ , $\sigma^*$ ), and (n, $\pi$ ) doubly excited states along the reaction path. The (n, $\pi$ ) state connects to a double transition from the nonbonding orbital of O<sub>3</sub> and the p- $\pi$  conjugating orbital (p of O<sub>24</sub> and  $\pi$  of benzothiazol) to the O<sub>3</sub>-O<sub>4</sub>  $\sigma^*$  orbital (see Chart 2). In addition, the ( $\pi$ , $\pi^*$ ) state changes to the ( $\pi$ , $\sigma^*$ ) state along the reaction path.

Therefore, we denoted the lowest three singlet states as  ${}^{1}(\sigma,\sigma^{*})$ ,  ${}^{1}(\pi,\pi^{*})/{}^{1}(\pi,\sigma^{*})$ , and  ${}^{1}(n,\sigma^{*})/{}^{1}(n,\pi)$  and the lowest triplet state as  ${}^{3}(\pi,\pi^{*})/{}^{3}(\pi,\sigma^{*})$  for FDO<sup>-</sup>. The adiabatic and diabatic PECs and the population of the Mulliken charges on the CO<sub>2</sub> and OxyLH<sup>-</sup> moieties of FDO<sup>-</sup> were calculated using the CASPT2//CAM-B3LYP method and are described on the right side of Figure 2.

The comparison of the  $S_0$  PECs calculated at the CAM-B3LYP, CAM-B3LYP with Yamaguchi's spin correction, and

Chart 2.  $(n,\pi)$  Doubly Excitation



CASPT2 methods for both **FDOH** and **FDO**<sup>-</sup> is shown in Figure S12. The CT and BCT processes on the PECs of **FDO**<sup>-</sup> are shown in Figures S13 and 3 using the CAM-B3LYP and CASPT2 methods, respectively.

The solvent effect of benzene and DMSO on the  $S_0$  PECs of **FDOH** and **FDO**<sup>-</sup> was considered using the CAM-B3LYP method and is shown in Figure S14. The charge population of the CO<sub>2</sub> and OxyLH<sub>2</sub>/OxyLH<sup>-</sup> moieties along the reaction coordinate is shown in Figure S15.

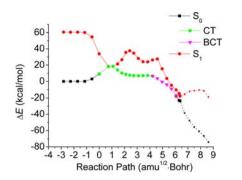


Figure 3. The CT and BCT processes on the PECs of FDO<sup>-</sup> calculated by the CASPT2//CAM-B3LYP method.

## DISCUSSION

**1.** Chemiluminescent Decomposition Process for FDOH. The decomposition of FDOH is initiated by the dissociation of the  $O_3-O_4$  peroxide bond. The vibrational mode of the imaginary frequency of  $TS_{O-O}$  corresponds to the  $O_3-O_4$  stretch. The  $O_3-C_1-C_2-O_4$  ring remains nearly planar until the O-O bond is completely broken. Therefore, the  $O_3-C_1-C_2-O_4$  twisting mode barely contributes to the dissociation of the O-O bond. After cleavage of the  $O_3-O_4$  bond, the four-member ring can no longer maintain planarity (see Figure 1 and Table S1). The other TS,  $TS_{C-C}$ , corresponds to the cleavage of the  $C_1-C_2$  bond with a  $O_3-C_1-C_2-O_4$  dihedral angle of  $-30.8^\circ$ . Between  $TS_{O-O}$  and  $TS_{C-C}$ , the  ${}^1(\sigma,\sigma^*)$  PEC

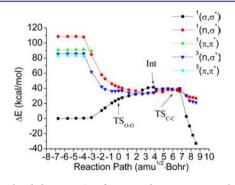
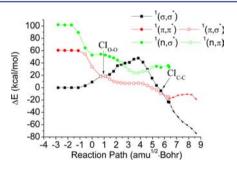


Figure 4. The diabatic PECs of FDOH decomposition calculated by the CASPT2//CAM-B3LYP method.

is flat (Figure S11A, Figure 2A and B, and Figure 4), and the  $(\sigma, \sigma^*)$  state in this area exhibits typical biradical characteristics  $(\langle S^2 \rangle \approx 1)$ . An Int between TS<sub>O-O</sub> and TS<sub>C-C</sub> was located and exhibited  $(n,\sigma^*)$  characteristics. The comparison of the three types of PECs is shown in Figure S12. According to the orbital analysis (Figures S2-S6), the biradical region primarily corresponds to the  ${}^{1}(n,\sigma^{*})$  state, and the out-plane p orbital of O<sub>3</sub> and the in-plane p orbital of O<sub>4</sub> are singly occupied. As shown in Figure 4, along the long and flat biradical region, the PESs of the  $(\sigma, \sigma^*)$  and  $(n, \sigma^*)$  states are degenerate or are nearly degenerate, which provides infinite possibilities for FDOH to change state. This path represents an entropic trapping, a crossing seam region for FDOH. The entire section of the path is degenerate. Let us specifically check the energy difference of the  ${}^{1}(\sigma,\sigma^{*})$  and  ${}^{1}(n,\sigma^{*})$  states at IRC = 0.00, 3.86, and 6.77 amu<sup>1/2</sup> bohr, which are 0.692, 0.289, and 0.286 eV, respectively. This is the reason that the CIs between the  ${}^{1}(\sigma,\sigma^{*})$  and  ${}^{1}(n,\sigma^{*})$  PESs were not located. The  ${}^{3}(n,\sigma^{*})$  state is

nearly degenerate with the  ${}^{1}(\sigma,\sigma^{*})$  and  ${}^{1}(n,\sigma^{*})$  states along the long and flat biradical region. We calculated the spin-orbital coupling (SOC) of the above three points on the flat region, and the values are shown in Tables S4, S5, and S6, respectively. According to El-Sayed's rule,<sup>35</sup> the ISC between  $(\sigma, \sigma^*)$  and  $^{3}(n,\sigma^{*})$  is allowed, but the ISC between  $^{1}(n,\sigma^{*})$  and  $^{3}(n,\sigma^{*})$  is forbidden in zero order. The FDOH chemiluminescence process is briefly described below. As shown in the reaction path in Figure 4, the reactant, FDOH in the  ${}^{1}(\sigma,\sigma^{*})$  state, changes to the  ${}^{1}(n,\sigma^{*})$  state via an entropic trap, and the  $^{1}(n,\sigma^{*})$  state leads to the product of the S<sub>1</sub>-state oxyluciferin and CO<sub>2</sub>, which subsequently produces chemiluminescence when the  $S_1$ -state oxyluciferin decays to its  $S_0$  state. Alternatively, FDOH may transfer back to the closed-shell  $^{1}(\sigma,\sigma^{*})$  state near TS<sub>C-C</sub> via the entropic trap leading to the product of the S<sub>0</sub>-state oxyluciferin and CO<sub>2</sub>. Meanwhile, the entropic trap also provides a high probability for intersystem crossing from the  ${}^{1}(\sigma,\sigma^{*})$  state to the  ${}^{3}(n,\sigma^{*})$  state, which will produce a large amount of triplet product without fluorescent activity. The decomposition process of FDOH is similar to its small analogues, which exhibit an asynchronous two-step reaction (e.g., Figure 1 in ref 8f and Figure 3 in ref 8g). The PECs in Figure S12A clearly show the systematic error of the CAM-B3LP when describing the biradical.

**2.** Chemiluminescent Decomposition Process for FDO<sup>-</sup>. Next, we discuss the decomposition process of FDO<sup>-</sup> based on the (TD) (BS)-CAM-B3LYP and CASPT2 calculated PECs (Figures 2, 5, S11, and S16) and the orbital population



**Figure 5.** The diabatic PECs of **FDO**<sup>-</sup> decomposition calculated using the CASPT2//CAM-B3LYP method.

using the CAM-B3LYP and CASSCF methods (Figures S2 and S7-S10). As shown in Figure 1, the decomposition of FDO<sup>-</sup> also starts with stretching of the O<sub>3</sub>-O<sub>4</sub> bond. During the decomposition of FDO<sup>-</sup>, there is only one TS, TS<sub>O-O</sub>. As its CAM-B3LYP optimized geometry shown in Table S1, TS<sub>O-O</sub> has an  $O_3 - O_4$  bond length of 1.753 Å. The  $C_1 - C_2$  bond does not vary significantly (1.55-1.65 Å) prior to the complete cleavage of the O3-O4 bond. The currently located FDO-TS<sub>0-0</sub> is different from the CASSCF located TS of the thiazole-substituted dioxtanone,<sup>8g</sup> whose C-C and O-O bonds are both evidently elongated. Therefore, the dissociation of  $C_1-C_2$  and  $O_3-O_4$  is an asynchronous process for the  $FDO^-$  decomposition. Analysis of the orbital and charge population in Figure S11 shows that TS<sub>O-O</sub> exhibits partial CT characteristics. Before the  $TS_{O-O}$ ,  $S_0$  primarily exists in a closedshell  ${}^1(\sigma,\sigma^*)$  state, while a typical  ${}^1(\pi,\sigma^*)$  CT state exists beyond the TS<sub>O-O</sub>. The occupation numbers of the orbitals indicate that the CT state is a biradical state where the  $p-\pi$ conjugation orbital of benzothiazol and in-plane p orbital of O<sub>3</sub> are singly occupied, the in-plane p orbital of O<sub>4</sub> is nearly double

occupied, and the negative charge primarily resides on the O<sub>4</sub> of the CO<sub>2</sub> moiety. The charge population of FDO<sup>-</sup> biradical is different from that of neutral biradical of FDOH, whose inplane p orbitals on O<sub>3</sub> and O<sub>4</sub> are singly occupied. According to Figures 5 and S16, there could be a CI (denoted as  $CI_{0-0}$ ) between the PESs of the  ${}^{1}(\sigma,\sigma^{*})$  and  ${}^{1}(\pi,\sigma^{*})$  states close to TS<sub>0-0</sub>. The CI<sub>0-0</sub> was located using the SA-CASSCF method with 14.4 kcal/mol energy relative to the minimum of the  $^{1}(\sigma,\sigma^{*})$  state. After TS<sub>O-O</sub>, the O<sub>3</sub>-O<sub>4</sub> distance continues to elongate, but the  $C_1-C_2$  bond does not dissociate until the  $O_3 - O_4$  distance elongates to approximately 2.1 Å. With the dissociation of  $C_1 - C_2$ , there exists the other CI between the PESs of the  ${}^{1}(\sigma,\sigma^{*})$  and  ${}^{1}(\pi,\sigma^{*})$  states (denoted as CI<sub>C-C</sub>), which was located using the SA-CASSCF method. The two branches after the CI<sub>C-C</sub> include the  ${}^{1}(\sigma,\sigma^{*})$  PES, which goes downhill rapidly to the ground-state product, and the  $(\pi, \sigma^*)$ PES, which leads to the product of the S<sub>1</sub>-state oxyluciferin and CO<sub>2</sub>, producing chemiluminescence when the S<sub>1</sub>-state oxyluciferin decays to its S<sub>0</sub> state. The decomposition of FDO<sup>-</sup> occurs via a CT induced asynchronous-concerted process (Figure 2E), which has a completely different mechanism from the decomposition of FDOH. In Figure S16, according to El-Sayed's rule, the ISC between  ${}^{1}(\sigma,\sigma^{*})$  and  ${}^{3}(\pi,\sigma^{*})$  is allowed, but the ISC between  ${}^{1}(\pi,\sigma^{*})$  and  ${}^{3}(\pi,\sigma^{*})$  is forbidden in zero order.

3. CIEEL or CTIL? Koo and Schuster<sup>5</sup> first proposed the CIEEL mechanism when they studied the thermolysis of a dilute solution of diphenoyl peroxide in 1977. There was no chemiluminescence when diphenoyl peroxide decomposed to benzocoumarin in CH<sub>2</sub>Cl<sub>2</sub>. However, the addition of specific aromatic hydrocarbons to the reaction mixture resulted in efficient light emission. They described the CIEEL mechanism in two steps. The initiating step is a CT process from the aromatic hydrocarbon to the peroxide to form a radical ion pair. The second step is a BCT from the radical anion to the radical cation of the aromatic hydrocarbon to generate the electronically excited singlet state of the hydrocarbon. Herein, we must remember two points regarding the initial meaning of the CIEEL mechanism. First, it is an intermolecular mechanism that produces an excited-state hydrocarbon, not an excited-state carbonyl compound (the thermolysis product of peroxides). Second, the formation of the radical ion pair is the key step for the CIEEL process. The related CT from the aromatic hydrocarbon to the peroxide and the BCT from the radical anion to the radical cation of the aromatic hydrocarbon are all full single CT processes. Since its proposal, the decomposition of peroxides to excited-state carbonyl compounds has been explained via the intramolecular CIEEL mechanism. As Matsumoto said, "The original acronym 'CIEEL' refers only to the chemiluminescence produced via the ET/BET mechanisms. However, CIEEL is now often being used loosely to indicate the chemiluminescent decomposition of a peroxide (high-energy molecule) induced by CT from a fluorescer that acts as an electron donor, even if it involves neither full single ET nor BET process."36

For the decomposition of **FDOH**, according to the population of Mulliken charges in Figures S11B and 2C, CT and BCT processes do not occur during the decomposition. The CIEEL or CTIL mechanism is not viable for the **FDOH** decomposition. On the basis of the above discussion, we have drawn the conclusion that the chemiluminescent mechanism of neutral dioxetanone occurs via an entropic trap. For the decomposition of **FDO**<sup>-</sup>, the CT and BCT process are clearly

visible in Figure 3. As shown in Figure 2F,  $\rho(\text{OxyLH}^-)$ gradually decreases from -0.96 to -0.28 along the IRC from 0.00 to 3.83 amu<sup>1/2</sup> bohr; simultaneously,  $\rho(\text{CO}_2)$  gradually increases from -0.04 to -0.72, which is the CT process.  $\rho(\text{OxyLH}^-)$  increases from -0.28 to -0.91, and  $\rho(\text{CO}_2)$ gradually decreases from -0.71 to -0.08 along the IRC from 3.83 to 6.07 amu<sup>1/2</sup> bohr, which is the BCT process. Both CT and BCT are gradual, not full one-electron CT processes. Therefore, there is no clear radical anion pair as required by the CIEEL mechanism, and it is inaccurate to describe the chemiluminescence of **FDO**<sup>-</sup> using the original definition of CIEEL mechanism. As described above, we may use a more accurate acronym (gradually reversible CT initiated luminescence (GRCTIL)) to describe the chemiluminescent mechanism of anionic dioxetanone.

**4. Solvent Effect.** The above discussion does not consider solvent effects. According to the PECs in Figure S14, the solvents barely affects the  $S_0$  PECs of **FDOH** and the closed-shell  $S_0$  of **FDO**<sup>-</sup>. However, the solvent effect clearly decreases the energies of the  $S_0$  PEC in the CT region for **FDO**<sup>-</sup>. The solvent effect on the charge population is shown in Figure S15. When the solvent polarity increases, the negative charge of CO<sub>2</sub> moiety increases for both **FDOH** and **FDO**<sup>-</sup>, which indicates that the solvent polarity causes the negative charge to accumulate on the CO<sub>2</sub> fragment. As Isobe indicated, the solvent polarity is favorable to neutral/radical pair production, but it is disadvantageous for the efficiency of the BCT process.<sup>10</sup>

5. Activation Barrier of Chemiluminescence. The activation barrier for the FDO chemiluminescence process is the energy that the reactant has to overcome to enter the  $S_1$ PES. The activation barrier is the relative energy ( $\Delta E^{\ddagger}$ ) from  $TS_{O-O}$  and  $CI_{O-O}$  to the minimum of the  $(\sigma, \sigma^*)$  state for **FDOH** and **FDO**<sup>-</sup>, respectively. The CASPT2 calculated  $\Delta E^{\ddagger}$ is 25.8 and 14.4 kcal/mol for  $TS_{0-0}$  of FDOH and FDO<sup>-</sup>, respectively. There are no available experimental activation energies for FDOH and FDO-. We have listed the experimental activation energies for the decomposition of 10 analogues of FDOH and FDO<sup>-</sup> (Chart S2) in Table S7. In general, their activation energies are 16-24 kcal/mol. The previously calculated  $\Delta E^{\ddagger}$  value of 19.7 kcal/mol<sup>10</sup> for FDOH using B3LYP/6-31+G\* is reasonable. However, the calculated  $\Delta E^{\ddagger}$  values of FDO<sup>-</sup> using B3LYP/6-31+G\* and CASPT2// SA-CASSCF/6-31G\* are 5.1<sup>10</sup> and 1.5 kcal/mol,<sup>15</sup> which are obviously stray, due to the inaccuracy of the energy obtained from the B3LYP method and the insufficient active space of the CASPT2 method, respectively. The difference between the activation energies for FDOH and FDO- indicates that the deprotonation is necessary for efficient firefly bioluminescence.

## CONCLUSION

The decomposition mechanism and pathway of the firefly dioxetanone have not been previously studied at a reliable theoretical level due to the challenging decomposition process that includes biradical, CT, and several nearly degenerated states, which require multireference methods for simultaneously considering several states with an active space available to the whole reaction process. We have investigated the thermolysis of firefly dioxetanone in both its neutral (**FDOH**) and anionic (**FDO**<sup>-</sup>) forms in the gas phase using CASPT2 theories in conjunction with the S<sub>0</sub> reaction path calculated with the DFT CAM-B3LYP method. The solvent effect on the S<sub>0</sub> reaction path is considered using the CAM-B3LYP method with PCM

and C-PCM models. The size of the chosen active spaces (16in-13 for FDOH and 18-in-15 for FDO<sup>-</sup>) with the assistance of state-average technique has been adequately validated for handling the whole reaction process involved in the decompositions of FDOH and FDO-. The decomposition of FDOH requires a two-step pathway with two TSs connected by an Int, while FDO<sup>-</sup> decomposes by an asynchronous two-stage pathway with only one CT TS without a discrete Int. The chemiluminescent mechanism of FDOH is similar to that of the small analogues previously studied, which have S<sub>0</sub>, T<sub>1</sub>, and S<sub>1</sub> states that are nearly degenerate in the biradical region and lead to nonadiabatic transitions. For FDO<sup>-</sup>, the double crossing of the potential energy surfaces of the S<sub>0</sub> and S<sub>1</sub> states indicates another chemiluminescent mechanism, which is different from the small analogues of FDO<sup>-</sup> previously studied and FDOH. The chemiluminescent decomposition of both FDOH and FDO<sup>-</sup> cannot be interpreted using the CIEEL mechanism. For FDOH, an entropic trap leads to an excited-state carbonyl compound. For FDO-, a more accurate mechanism denoted the gradually reversible CT initiated luminescence (GRCTIL) mechanism has been proposed. The activation energy of FDOis 11.4 kcal/mol smaller than that of FDOH based on the CASPT2 calculations, which also indicates that the deprotonation is required for efficient firefly bioluminescence.

# ASSOCIATED CONTENT

#### **Supporting Information**

Active orbitals and natural orbitals; the comparison between geometric structures optimized using different basis sets; the important geometric parameters of stationary points; the CASPT2 calculated relative energy of the stationary points of **FDOH** and **FDO**<sup>-</sup>; the natural orbitals and occupation numbers for the important orbitals of Min,  $TS_{O-O}$ , Int, and  $TS_{C-C}$  of **FDOH**, and of Min,  $TS_{O-O}$ , and  $CI_{O-O}$  of **FDO**<sup>-</sup>; the comparison of key geometric parameters of Min and TS optimized by CAM-B3LYP and B3LYP; S<sub>0</sub> PECs in solvent based on CAM-B3LYP IRC; spin—orbit coupling of **FDOH** at selected points; the experimental activation energy of some dioxetane derivatives; the Cartesian coordinates and absolute energy for all of the key structures. This material is available free of charge via the Internet at http://pubs.acs.org.

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# Notes

The authors declare no competing financial interest.

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